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	One sample case for the mean			One sample case for the correlation			
	Z-Test: Known Population Variance (σ^2) (uncommon)	T-Test: Unknown Population Variance (σ^2)	SPSS	Known population correlation (uncommon)	Unknown population correlation		SPSS
State the null hypothesis	$H_0: \mu=100$ (or something)	$H_0: \mu=162$ (or something) $H_a: \mu \neq 162$ (non directional)	<i>Go to Analyze, Compare Means, One Sample T-Test</i>	$H_0: \rho=a$ (is the correlation the same as the population?) $H_0: \rho=0.35$ $H_a: \rho \neq 0.35$	$H_0: \rho=0$ $H_a: \rho \neq 0$ <i>Is the correlation significantly different from 0?</i>	<i>alternative method</i> $H_0: \rho=0$ $H_a: \rho \neq 0$	<i>Go to Analyze, Correlate, Bivariate</i>
Set the criteria for rejecting the null	$(\alpha) = 0.05$ Critical value = 1.96 for a two tailed test or 1.645 for a one tailed test. <i>See also Table 8.1 p. 189</i> <i>Based on normal distribution</i>	$(\alpha) = 0.05$ Critical value = Look at Table C3 Use n-1 for df <i>Based on Student's t distribution</i>	$(\alpha) = 0.05$	$(\alpha) = 0.05$ Critical value = 1.96 for a two tailed test or 1.645 for a one tailed test. <i>See Table 8.1 p189</i> <i>Based on normal distribution</i>	$(\alpha) = 0.05$ Critical value = Look it up on Table C3 Use n-2 for df <i>Based on Student's t distribution</i>	$(\alpha) = 0.05$ Critical value = Look it up on Table C3 Use n-2 for df	$(\alpha) = 0.05$
Compute the test statistics	<i>Z-test for the one sample mean</i> $Z = \frac{x - \mu}{\sigma_m}$ $\sigma_m = \frac{\sigma}{\sqrt{n}}$	<i>t-test for the one sample mean</i> $t = \frac{x - \mu}{S_m}$ $S_m = \frac{S}{\sqrt{n}}$	Look for the p value in the sig. (2 tailed) column.	$Z = \frac{Z_r - Z_p}{S_{zr}}$ Use Table C6 to convert r to Fisher's Z (Zr) $S_{zr} = \sqrt{1/(n-3)}$	$t = r\sqrt{\frac{(n-2)}{(1-r^2)}}$		Look for the p value in the sig. (2 tailed) row. (It's the % error you make if you reject the null.
Construct a confidence interval	(CI) = Statistic (X) +/- (critical value x standard error of the statistic) 95% if we set $(\alpha) = 0.05$	CI = X +/- (CV) (Sm)		CI = Zr +/- (CV) (S _{zr})	CI = Zr +/- (CV) (S _{zr}) Use Table C6 to convert r to Zr and then when done to convert both interval endpoints back to r		
Make a decision	If the Z score is less than CV, retain the null. If the Z score is greater than the CV, reject the null.	If the t score is less than CV, retain the null. If the t score is greater than the CV, reject the null.	Compare p value to $(\alpha) = 0.05$. If it is greater, reject the null.	If the Z score is less than CV, retain the null. If the Z score is greater than the CV, reject the null.	If the t score is less than CV, retain the null. If the t score is greater than the CV, reject the null. If the hypothesized correlation is outside the CI ₉₅ , reject the null.	If ρ is greater than the CV, it is significantly different than 0. If ρ is less than the CV, it is not significantly different than 0.	Compare p value to $(\alpha) = 0.05$. If it is 0.05 or less, reject the null.
Effect Size		$d = \frac{\text{mean difference}}{\text{standard deviation}}$ 0.2 small 0.5 medium 0.8 large					
Notes	x = sample mean μ = population / hypothesized mean σ_m = Standard error of the mean	df = degrees of freedom d= effect size S = standard deviation					

Two sample case for the mean							
	FIRST Test <i>homogeneity of variance</i>	t-test for independent samples homogeneity of variance assumed	SPSS	t-test for independent samples homogeneity of variance NOT assumed	SPSS	t-test for dependent samples (or correlated samples) examples: pretest/ posttest; husbands / wives; twins, etc. n = number of paired observations	SPSS
Assump- tions	Independent samples: scores in one group are not influenced by scores in other group Homogeneity of variance: variances in the population are equal. $\sigma_1^2 = \sigma_2^2$	1 st test if we meet the homogeneity of variance assumption (see column 1)	<i>Go to Analyze, Compare Means, Independent Samples T-Test Test variable is the continuous variable; grouping variable is the two groups.</i>	1 st test if we meet the homogeneity of variance assumption (see column 1) <i>df is different standard error is different</i>	<i>Analyze, Compare Means, Independent Samples T-Test</i> Look under Levine's test for Sig. If $p > 0.05$ or α , assume homogeneity. Read the row that matches the homogeneity results (bottom row for no homogeneity)		<i>Go to Analyze, Compare Means, Paired-Samples T Test Add the two variables.</i>
Hypo- thesis	Ho: $\sigma_1^2 = \sigma_2^2$ (desired outcome)	Ho: $\mu_1 = \mu_2$ or Ho: $\mu_1 - \mu_2 = 0$ Ha: $\mu_1 \neq \mu_2$ or Ha: $\mu_1 - \mu_2 \neq 0$	Look under Levine's test for Sig. If $p > 0.05$ or α , assume homogeneity.	H0: $\mu_1 = \mu_2$ Ha: $\mu_1 \neq \mu_2$		H0: $\mu_1 - \mu_2 = d = 0$ Ha: $\mu_1 \neq \mu_2$	
Criteria for rejecting null	(α) = 0.05 Fcv two dfs: $n_1 - 1$ and $n_2 - 1$ <i>Based on F distribution (Table C5)</i>	(α) = 0.05 or 0.01 Look at Table C3 df = $n_1 + n_2 - 2$ <i>Based on t-distribution</i>	Read the row that matches the homogeneity results (top row for homogeneity).	df = $\frac{[(S_1^2/n_1) + (S_2^2/n_2)]^2}{[(S_1^2/n_1)/(n_1-1)] + [(S_2^2/n_2)/(n_2-1)]}$ Look at Table C3 <i>Based on t-distribution</i>		(α) = 0.05 / 0.01 df = $n - 1$ Table C3 <i>Based on t-distribution</i>	
Test Statistic	Ratio between the variances Put the larger number in the numerator $F = \frac{S_1^2 (\text{largest})}{S_2^2 (\text{smallest})}$ Remember that S^2 is the variance.	find: $s^2 = \frac{[\sum X_1^2 - (\sum X_1)^2 / n_1] + [\sum X_2^2 - (\sum X_2)^2 / n_2]}{n_1 + n_2 - 2}$ then find: $S_{m1-m2} = \sqrt{[s^2 (1/n_1 + 1/n_2)]}$ then find: $t = \frac{(M_1 - M_2)}{S_{m1-m2}}$		find: $S_{m1-m2} = \sqrt{[(S_1^2/n_1) + (S_2^2/n_2)]}$ then find $t = \frac{(M_1 - M_2)}{S_{m1-m2}}$		Find standard error $S_{md} = S_d / \sqrt{n}$ S_d = standard deviation of difference M_d = Mean of difference between pairs $t = M_d / S_{md}$	
CI	in SPSS, look at the sig for the F/Levene's test. If $p < 0.05$, reject null & assume no h. of pop.var.	(CI) = mean difference between groups $(M_1 - M_2) \pm t_{cv} \times S_{m1-m2}$	Look at the CI lower & upper.	(CI) = mean difference between groups $(M_1 - M_2) \pm t_{cv} \times S_{m1-m2}$	Look at the confidence interval lower & upper.	CI = $M_d \pm t_{cv} \times S_{md}$	
Effect Size (d)	remember: 0.2 small 0.5 medium 0.8 large	$\frac{M_1 - M_2}{s}$ where $s = \sqrt{s^2}$ or $d = t \sqrt{[(n_1 + n_2) / n_1 n_2]}$		$\frac{M_1 - M_2}{s}$ or $d = t \sqrt{[(n_1 + n_2) / n_1 n_2]}$		M_d / S_d or t / \sqrt{n}	
decision	If F is equal to or greater than Fcv, reject the null. (no homogeneity of variance)	If t is less than tcv, retain the null. If the hypothesized value (0) is within the interval, retain the null.	Look at Sig. (2- tailed). If $p > \alpha$, retain the null. If the CI contains 0, retain null.	If t is less tcv, retain the null. If the hypothesized value (0) is within the interval, retain the null.	Look at Sig. (2- tailed). If $p > \alpha$, retain the null. If the CI contains 0, retain the null.	If t is greater than tcv, reject the null. If CI does not contain 0, reject the null.	Look at Sig. (2- tailed). If p is greater than α , retain the null. If the CI contains 0, retain the null.
Notes	Independent variable (the two groups) Dependent variable – the continuous variable that the groups vary on (in theory)	m_1 = group 1 mean; m_2 = group 2; mean; $m_1 - m_2$ = absolute value of mean difference between groups S_{m1-m2} = standard error of the difference between the group means s^2 = pooled est. of pop variance	(α) = 0.05 or 0.01	remember $s = \sqrt{s^2}$	(α) = 0.05 or 0.01	Make a column to find the difference. Find the mean (M_d) and the std deviation (S_d)	(α) = 0.05 or 0.01

Linear Regression Steps	Conditional Distributions	Test Significance	SPSS (Thanks Cheryl Kisunzu)
<p><i>x is the independent variable; y is the dependent</i> Develop the regression equation using the method of least squares:</p> <p>1st calculate b. $b = \frac{n\sum XY - \sum X \sum Y}{n\sum X^2 - (\sum X)^2}$</p> <p>To get all these sums, go to SPSS, use Compute to create a variable column for XY; create another for X²; then go to Analyze, Descriptive Statistics, Descriptives.</p> <p>or for b use this: $b = r (S_y/S_x)$ (S is the standard deviation)</p> <p>Then calculate a. $a = \frac{\sum Y - b\sum X}{n}$</p> <p>Then plug the numbers into the regression equation: $Y' = a + bX$</p>	<p>Assumptions: The conditional distribution is normal. The mean of the distribution is the predicted score Y' The standard deviations of all the conditional distributions are equal (homoscedasticity). The standard deviation of the conditional distributions is the standard error of the estimate (S_{y.x})</p> <p><i>Probability of getting the predicted score or higher</i> $Z = (Y - Y') / S_{y.x}$</p> <p>Y – Criterion Variable Y' – the predicted score for each fixed value of X; or the mean of the distribution of Y for each value of X. S_{y.x} – Standard error of estimate or standard deviation of each conditional distribution</p> <p>Put the z score in the Normal Distribution Calculator or (Table C1) http://davidmlane.com/hyperstat/z_table.html</p> <p>Click radio box for above Z Read the shaded area and convert to % probability of getting that score.</p> <p><i>Probability of getting another score or higher</i> Same as above, put the “another score” in Y Click radio box for above Z <i>You're predicting y given x</i></p>	<p>In simple linear regression (only one predictor variable), if the correlation is significant, the regression coefficient is significant.</p> <p>Hypothesis H₀: β=0 (β is the population regression coefficient)</p> <p>Set Criterion (α) =0.05 or 0.01 Look at Table C3 df = n-2 <i>Based on t-distribution</i></p> <p>Test Statistics $t = (b - \beta) / S_b$ remember β=0</p> <p>$S_b = S_{y.x} / \sqrt{(n-1)S_x^2}$ Get S²_x from the SPSS sums. S_{y.x} See errors of prediction, left.</p> <p>Make Decision If t is greater than t_{cv}, the null must be rejected.</p> <p>----- x= independent / predictor y= dependent / criterion</p>	<p>Descriptives (means & std devs): To get all the sums you need, go to SPSS, use Compute to create a variable column for XY; create another for X²; then go to Analyze, Descriptive Statistics, Descriptives.</p> <p>Correlation Analyze, Correlate, Bivariate</p> <p>Linear Regression Analyze, Regression, Linear then click the dependent variable to move it into the dependent variable box; followed by clicking the independent variable and moving it into the independent variable box then click OK</p> <p>Scatterplot with regression line Graphs, Interactive, Scatterplot, check regression under Fit tab.</p> <p><i>How good is it?</i> Look at the Model Summary. R Square tells you how “good” it is; percent of variance in the criterion that’s explained by the predictor.</p>
<p>How good is it? Compute the square of the correlation between the criterion & predictor variables. Converted to percent, this indicates x percent of the criterion scores can be predicted by the predictor variable. (This is also called variance.)</p>			
<p>Is it significant? Is the correlation (r) statistically significant? Check p compared to 0.05 (should be less)</p>	<p>Confidence Intervals $CI = Y' \pm (t_{cv})S_{Y'}$</p>		
<p>Predicting scores Plug X into the regression equation. Y' = a + bX <i>Can do in SPSS or by hand.</i></p>	<p>Y' = predicted score t_{cv} – critical value for t for df n-2 (Table C3)</p> $S_{Y'} = S_{y.x} \sqrt{\{1 + (1/n) + \frac{[(X - \bar{X})^2]{(n-1)S_x^2}}{(n-1)S_x^2}\}}$		
<p>Errors of prediction / standard error of estimate Higher the correlation, the smaller the prediction/residual errors. To find the standard error of the estimate / the standard deviation of the distribution of errors of prediction: $S_{y.x} = S_y \sqrt{(1-r^2)} \sqrt{\frac{(n-1)}{(n-2)}} \quad (6.11)$ $S_{v.x} = S_y \sqrt{(1-r^2)} \quad (6.12 \text{ for large samples, } 30+)$</p>	<p>Look back at the all the numbers you got in SPSS in step 1 under Linear Regression to fill this in.</p>		
<p>Reminders: a = Y intercept = regression constant b = slope = regression coefficient</p>			

Chi-Square Tests of Frequencies

	Goodness-of-fit (one-sample case)	SPSS	Test of independence (or test of homogeneity or association)	SPSS	Test of Two-Dependent Samples or McNemar Test	SPSS
Assumptions	*one categorical/nominal variable *used to determine if there is relative agreement between observed frequencies and expected frequencies *expected frequencies come from the research scenario	You may have to reconstruct the data (enter the number of scores for each category).	*two nominal variables	You may have to reconstruct the data (enter the number of scores for each category).	Tests for significance of change. The non-parametric equivalent of the paired sample t-test. The frequencies are of a category instead of measurement along a continuous scale.	You may have to reconstruct the data (enter the number of scores for each category).
Hypothesis	Null: There is no difference between the categories. Or the categories fit an expected frequency. (stated in words, not symbols)	Analyze, nonparametric tests, chi-square.	Null: There is no relationship between the two variables or there is no difference among the categories.	Analyze, Descriptives, CrossTabs, under the Cells button check Observed, Expected & standardized residuals; under the Stats button check Chi-Square and Phi/Cramer's V. Then run it.	Null: An equal number of people change their mind from before to after.	Analyze, Descriptives, CrossTabs, under the Cells button check Observed, Expected & standardized residuals; under the Stats button check Chi-Square and Phi/Cramer's V. Then run it.
Criteria for rejecting null	$\alpha = 0.05$ $df = C - 1$ (C = number of categories) <i>If there are more than 30 categories, use formula 21.2:</i> $z = \sqrt{2} \chi^2 \cdot \sqrt{2df - 1}$ $\chi^2_{(cv)}$ Look up in Table C4 <i>based on Chi-Square distribution</i>	Asymp. Sig is the p value for the chi-square. If the p value is greater than our criterion of $\alpha = 0.05$, then we retain the null.	$\alpha = 0.05$ $df = (R - 1)(C - 1)$ R = # of rows C = # of columns $\chi^2_{(cv)}$ Look up in Table C4 <i>based on Chi-Square distribution</i>	Observed, Expected & standardized residuals; under the Stats button check Chi-Square and Phi/Cramer's V. Then run it.	$\alpha = 0.05$ $df = (R - 1)(C - 1)$ $\chi^2_{(cv)}$ Look up in Table C4 <i>based on Chi-Square distribution</i>	If the p value is greater than our criterion of $\alpha = 0.05$, then we retain the null.
Test Statistic	$\chi^2 = \sum \left[\frac{(O - E)^2}{E} \right]$ <i>(it should make a long formula for each instance - i.e. $(1-2)^2/2 + (2-3)^2/3 + \dots$)</i>		$\chi^2 = \sum \left[\frac{(O - E)^2}{E} \right]$ Expected frequencies are computed: $E = \frac{f_r \cdot x \cdot f_c}{N}$ <i>It's ok to get these in SPSS.</i>	If the p value is greater than our criterion of $\alpha = 0.05$, then we retain the null.	$\chi^2 = (A - D)^2 / (A + D)$ A & D are the cells representing changes (i.e. in opinion). It doesn't matter which is A or D.	
Decision	If the observed χ^2 is less than the critical value, retain the null.		If the observed χ^2 is less than the critical value, retain the null.		If the observed χ^2 is less than the critical value, retain the null.	
Effect Size	$ES = \chi^2 / (N)(K - 1)$ K = number of categories 0.10 - Small 0.30 - Moderate 0.50 - Large		Cramer's V is used as an index $ES = \sqrt{[(\chi^2/N) / ((\text{the smaller of } R \text{ or } C) - 1)]}$ R = # of rows C = # of columns		Effect size is the difference between the proportions of people who changed their opinion. Proportion is number who changed / N. Calculate for both. Then subtract the smaller from the larger.	
Standardized residual	$R = \frac{O - E}{\sqrt{E}}$ This determines the statistical significance. If the residual is greater than 2, it is a major contributor to the significant χ^2 value.		If the null is not rejected, there is no need to calculate standardized residuals. $R = \frac{O - E}{\sqrt{E}}$		Calculate for both. Then subtract the smaller from the larger. ----- $R = \frac{O - E}{\sqrt{E}}$	
Notes	O = Observed frequency E = Expected frequency					